

**MATH 131P: PARTIAL DIFFERENTIAL EQUATIONS
(WINTER 2019)**

Homework 9: due Wednesday, March 13

(This is the last assignment.)

- Lesson 27: 1, 2, 3.
- Lesson 33: 3, 5, 6, 7, 8.
- Lesson 34: 1.

Additional problem:

- (1) Consider the Neumann problem of the Laplace equation on the rectangle

$$\begin{aligned}u_{xx} + u_{yy} &= 0, & 0 < x < a, 0 < y < b \\u_x(0, y) &= 0, & u_x(a, y) = f(y), & 0 < y < b \\u_y(x, 0) &= 0, & u_y(x, b) = 0, & 0 \leq x \leq a.\end{aligned}$$

Find the solution using separation of variables. From the solution, deduce that if the solution exists, it is necessary that

$$\int_0^b f(y) dy = 0.$$