## MATH 250 HANDOUT 9 - MORE PROBLEMS ABOUT SETS; POWER SETS

Let A, B, and C be sets. Draw a Venn diagram demonstrating each of the following and then prove each of the following.

- (1) Prove that  $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$ .
- (2) Prove that  $A (B \cap C) = (A B) \cup (A C)$ .
- (3) Prove that  $(A B) \cup (B A) \subset (A \cup B) (A \cap B)$ .
- (4) Prove that if  $A B \subset C$ , then  $\overline{C} \subset \overline{A} \cup B$ .

Disprove each of the following statements by giving examples of sets A, B, C demonstrating that the statement is false. (I.e., give a counterexample.)

- (1) For all sets  $A, B, C, A \cup (B \cap C) = (A \cup B) \cap C$ .
- (2) For all sets  $A, B, C, A \cap (B \cup C) = (A \cap B) \cup C$ .
- (3) For all sets A, B, C, if A, B are subsets of C, then (C A) B = C (A B).
- (4) For all sets A, B, C, if A, B are subsets of C and if  $A \subset B$ , then  $(C A) \subset (C B)$ .

## Power Sets

- (1) Write our 4 elements of (1) P((0, 1, 2, 2, 4))
  - (a)  $P(\{0, 1, 2, 3, 4\});$
  - (b)  $P(\mathbb{N});$
  - (c)  $P(\mathbb{R})$ .

- (2) Let A = {0, 1, 2}. Circle whichever of the following statements are true.
  (a) {0} ⊂ P(A);
  - (b)  $\{1,2\} \in P(A);$
  - (c)  $\{\{0,1\},\{1\}\} \subset P(A);$
  - (d)  $\emptyset \in P(A);$
  - (e)  $\emptyset \subset P(A);$
  - (f)  $\{\emptyset\} \in P(A)$ .
  - (g)  $\{\emptyset\} \subset P(A);$
  - (h)  $\{1, \{1\}\} \subset P(A)$ .
- (3) Let A and B be sets. Prove or disprove:
  - (a)  $P(A) \cup P(B) \subset P(A \cup B)$ .
  - (b)  $P(A \cup B) \subset P(A) \cup P(B)$ .
  - (c)  $P(A) \times P(B) \subset P(A \times B)$ .
  - (d) A = B if and only if P(A) = P(B).